

# Modified Green-Ampt Method in EPA SWMM

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**CDM  
Smith**

# Overview

- History
  - Implementation in SWMM
  - Examples
  - Formulation
- Algorithm improvement
  - Anomalies
  - Identifying the error
  - Resolution
- Example

## Green-Ampt equation (1911)

$$f_p = K_s \left( 1 + \frac{\psi_s \theta_d}{F} \right) \quad \text{Eqn. 4-27}$$

$f_p$  = infiltration capacity, (in/hr)

$k_s$  = saturated hydraulic conductivity (in/hr)

$\psi_\theta$  = capillary suction (in)

$\theta_d$  = initial moisture deficit

$F$  = cumulative infiltration volume (in)

# Green-Ampt-Mein-Larsen (GAML)

- 1973: Mein-Larsen formulation for steady rainfall

Prior to saturation  $F < F_s$ ,  $f = i$ . Saturation occurs when

$$F_s = \frac{K_s \psi_s \theta_d}{i - K_s} > F$$

- 1978: Chu adaptation for unsteady rainfall
- 1979: Coded into SWMM 3 by R. Mein
- 1993-2002: Minor refactoring by W. Huber
- 2004: Re-coded in C by L. Rossman

# Tweaks 2005-2010

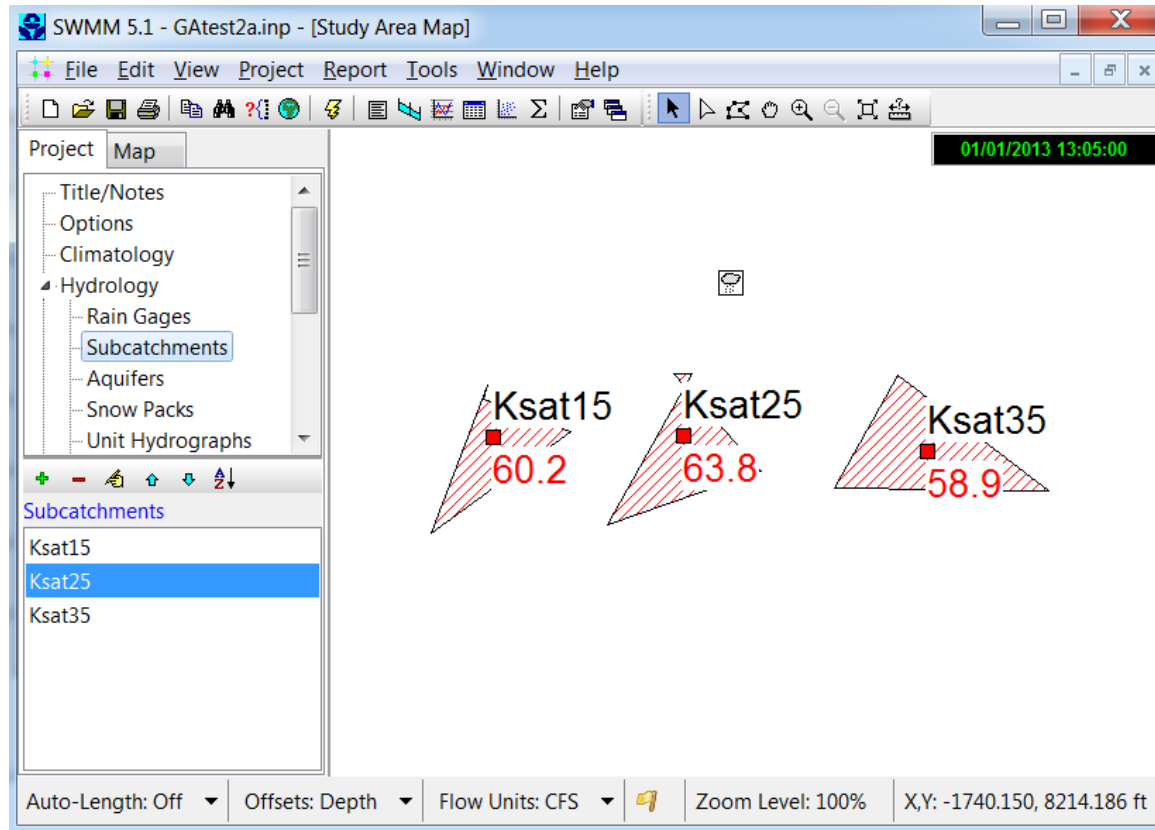
- Corrections to the way water volume in the upper soil zone is depleted during dry periods. 5.0.06 (2005)
- The point at which the time to drain the upper soil zone is first calculated was moved from time 0 to the time of first rainfall. 5.0.12 (2008)
- Infiltration rate corrected for the case when surface becomes saturated part way through current time step. 5.0.14 (2009)
- Explicitly include effect of ponded water depth on infiltration rate. 5.0.015 (2009)
- Infiltration rate no longer allowed to be less than smaller of saturated hydraulic conductivity and available surface moisture. 5.0.21 (2010)

# Model Comparison

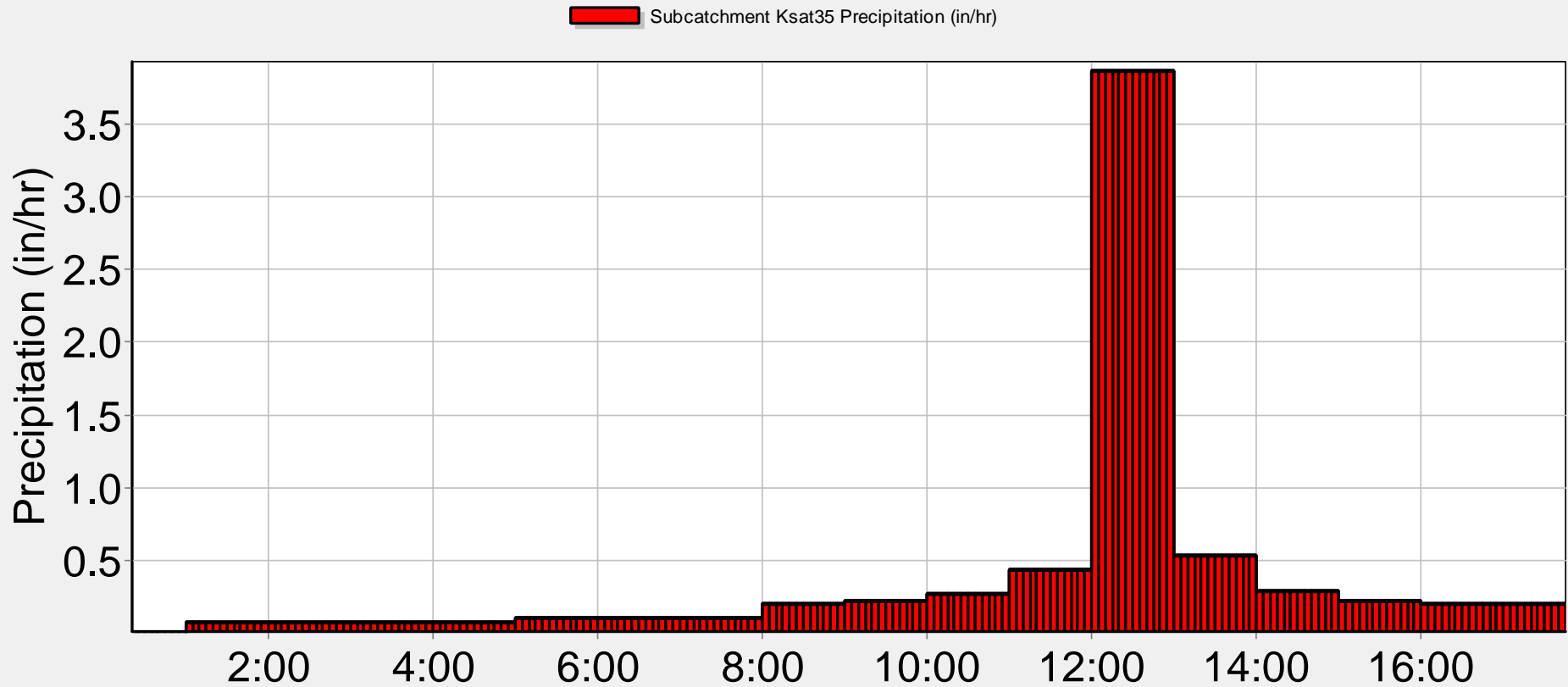
- Project technical memo
  - XPSWMM vs. EPA SWMM
  - Hydrology matches for Horton and NRCS infiltration, but not for Green-Ampt
  - XP Solutions noted that under certain conditions, EPA SWMM does not vary for changing capillary suction; CDM Smith independently confirmed this result

# Sensitivity Analysis

- Identical subbasins
  - 50 acres
  - 1000 ft width
  - 1% slope
  - Zero imperviousness
  - 0.25 pervious N
  - 6 inch NRCS Type II hyetograph
- Vary Ks, IMD, Su to pinpoint anomaly



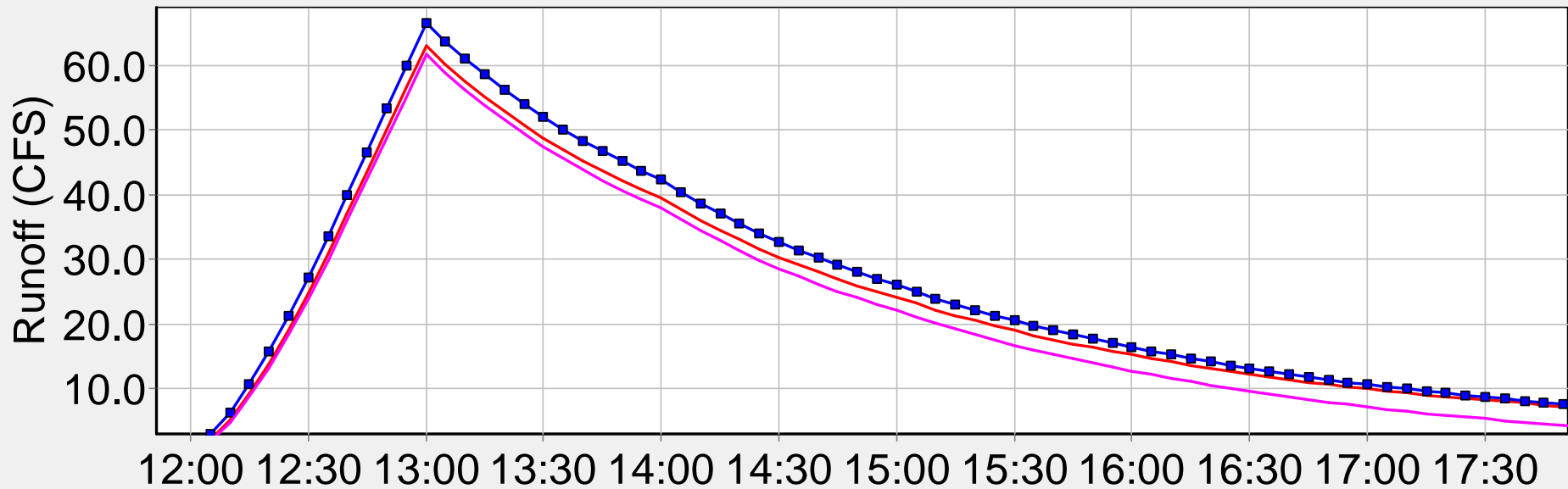
# Test model SWMM 5.1.006





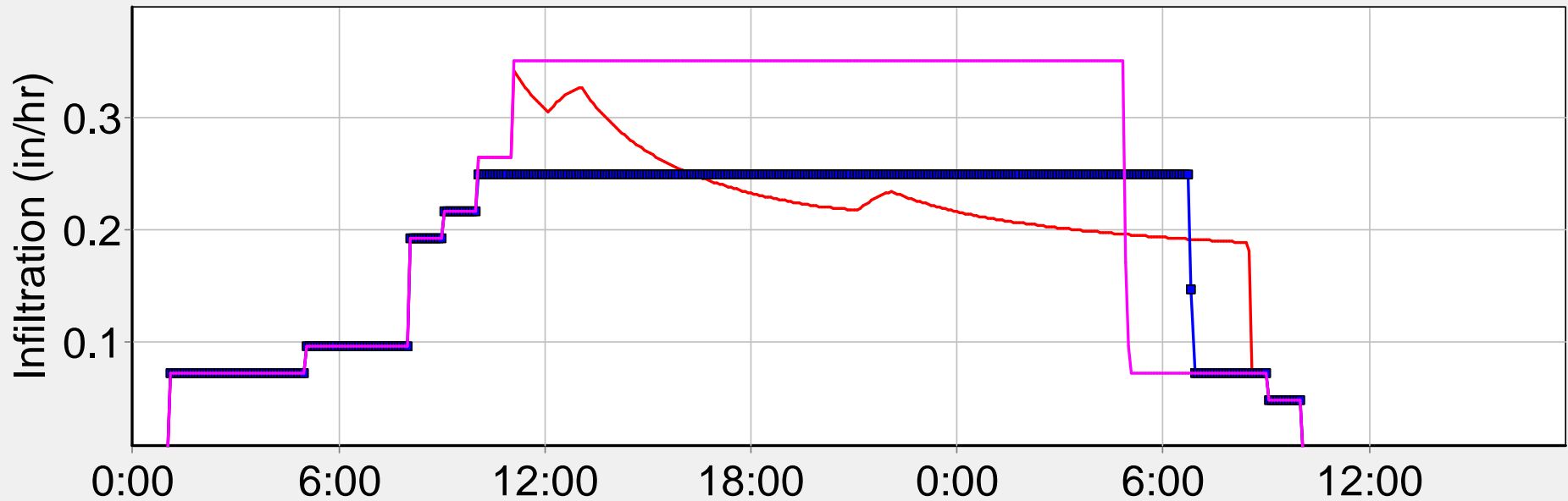
# Sensitivity Analysis

- Subcatchment Ksat15 Runoff (CFS)
- Subcatchment Ksat25 Runoff (CFS)
- Subcatchment Ksat35 Runoff (CFS)



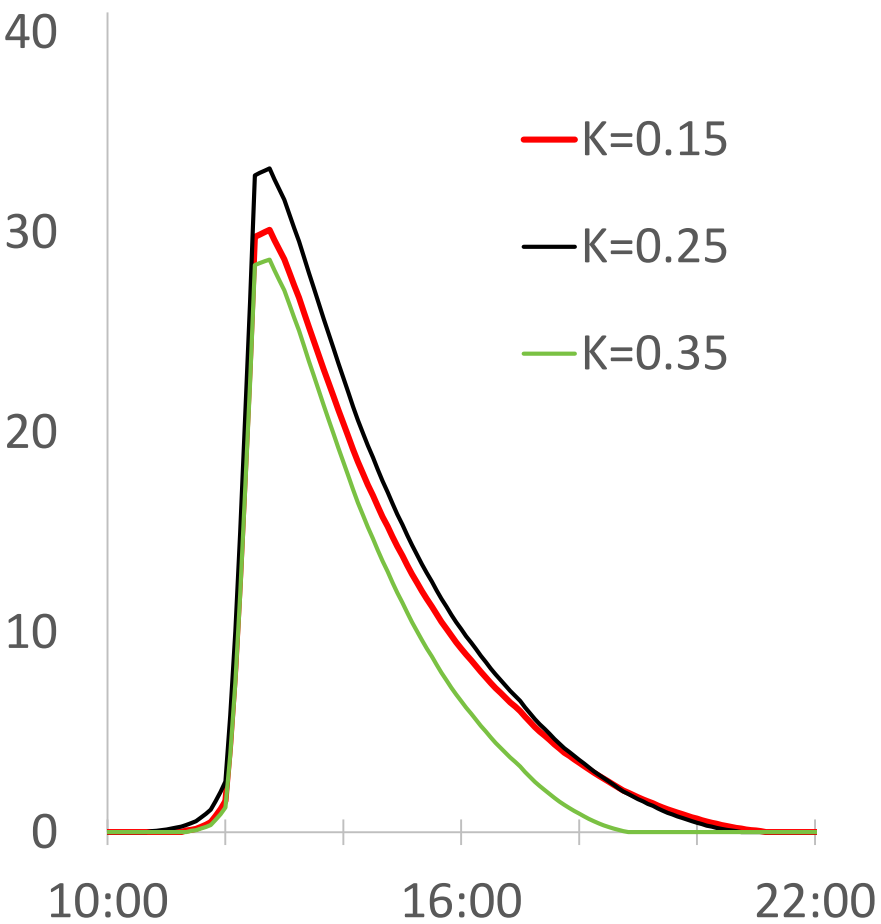
# Infiltration rate

- Subcatchment Ksat15 Infiltration (in/hr)
- Subcatchment Ksat25 Infiltration (in/hr)
- Subcatchment Ksat35 Infiltration (in/hr)

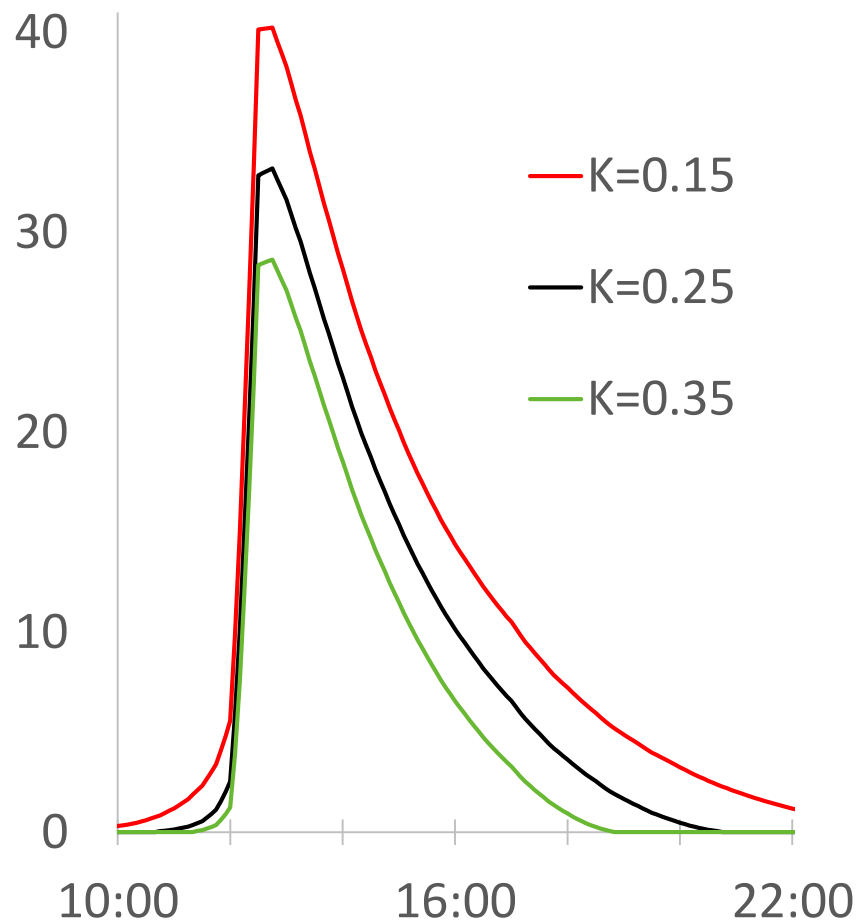


# Sensitivity Analysis

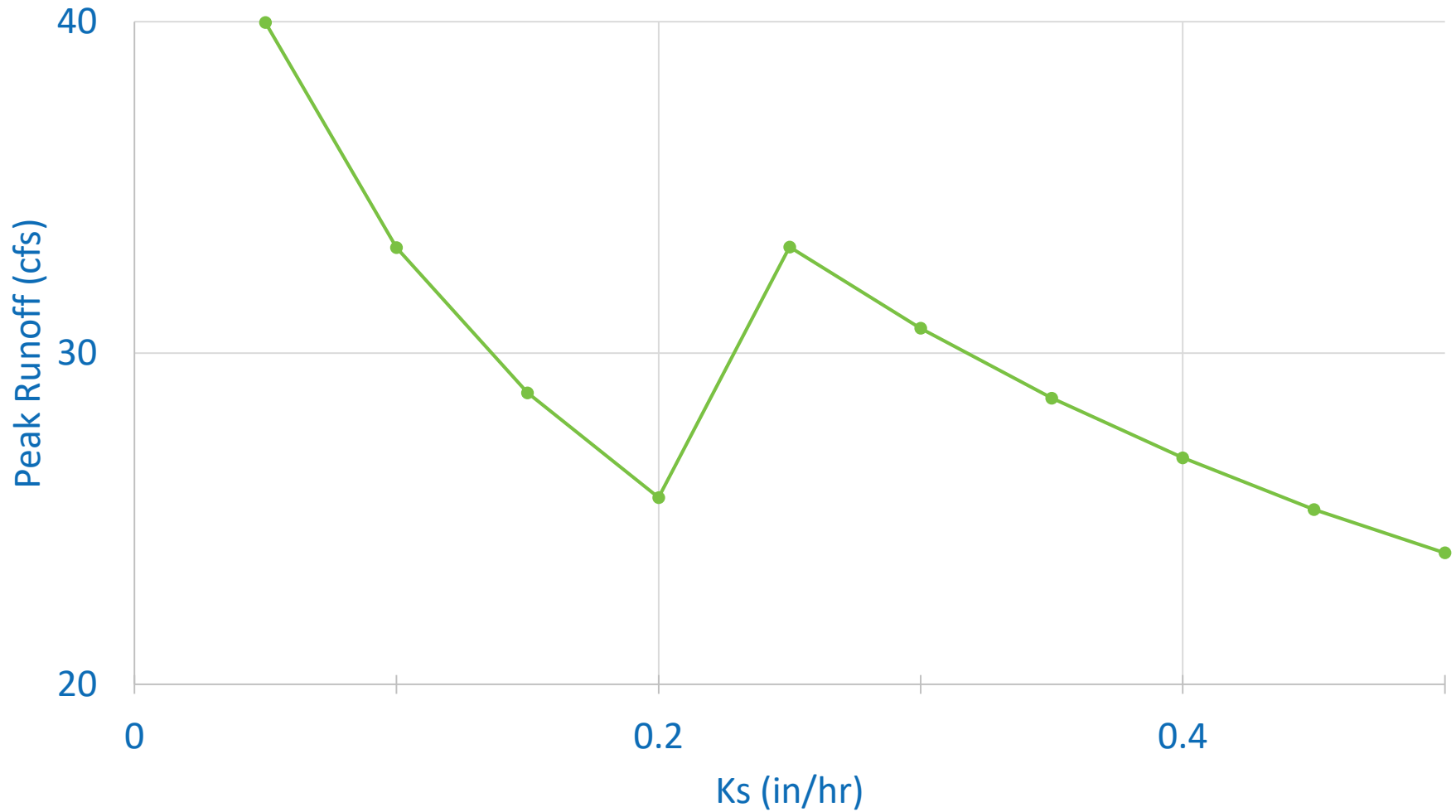
## Cold start



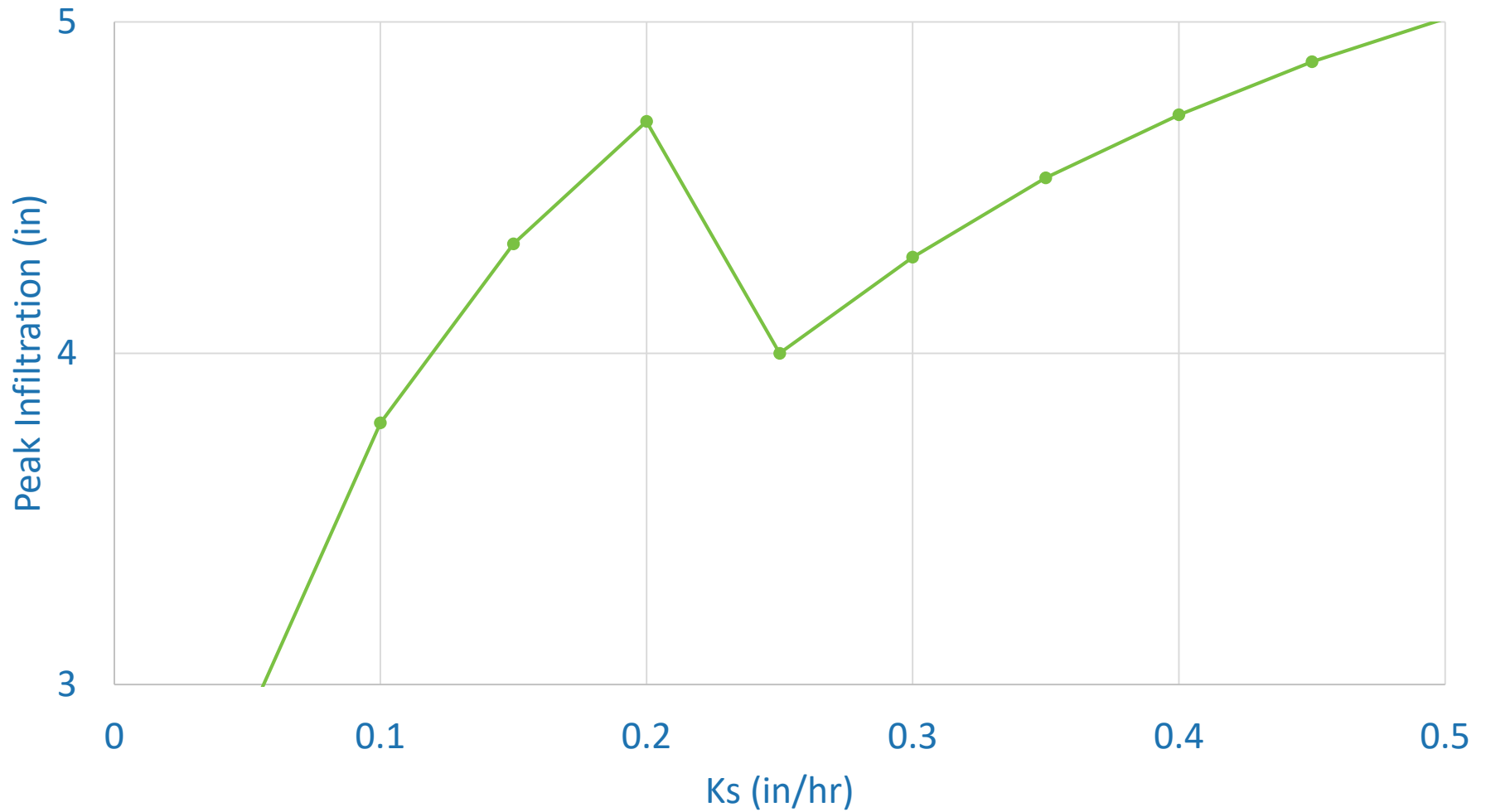
## Warmed up



# Sensitivity analysis

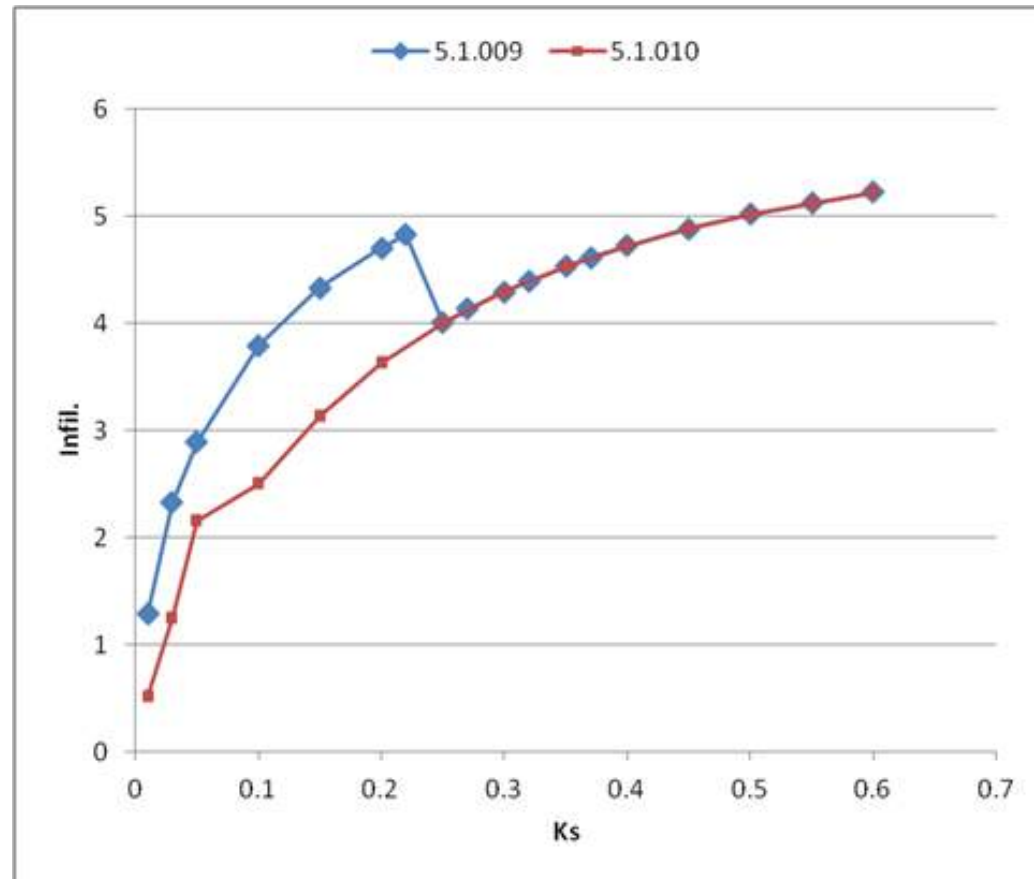


# Sensitivity Analysis



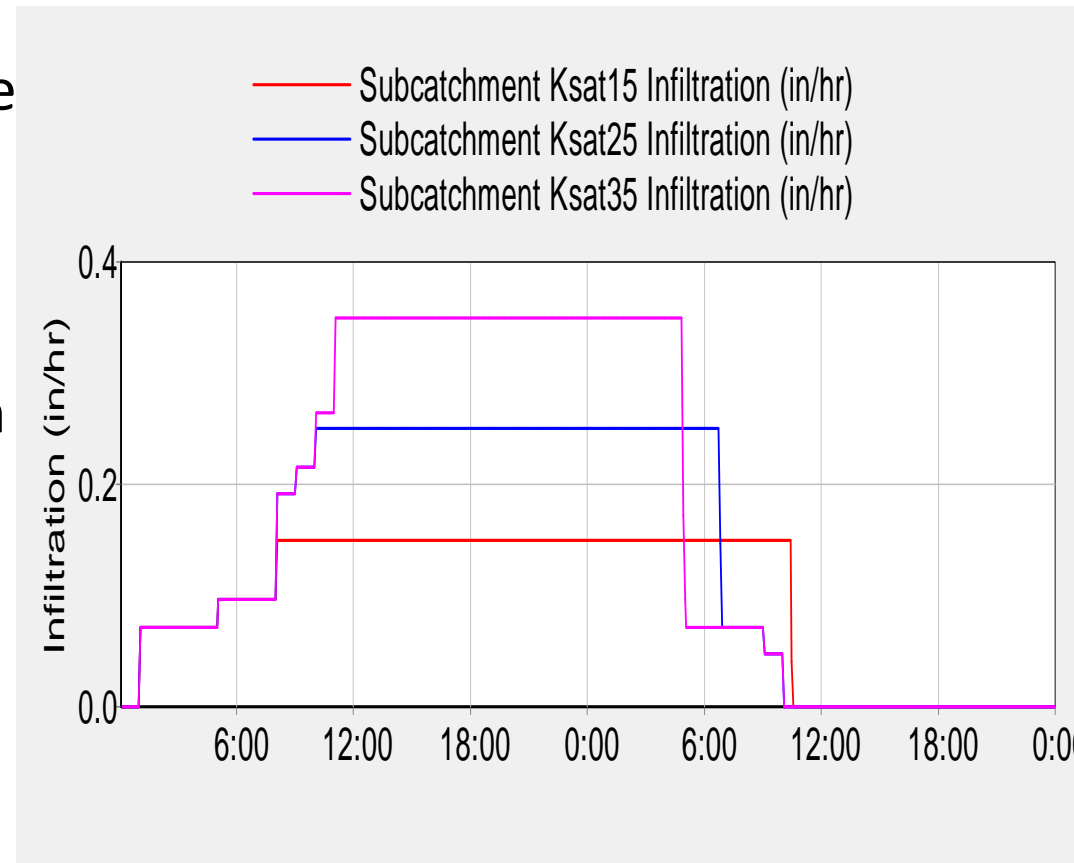
# SWMM 5.1.010 vs SWMM 4.4

- Differences in the code between earlier and current versions of SWMM
  - Event separation time initialization
  - Solver convergence limits
- Base Green-Ampt infiltration in SWMM 5.1.010 revises the methodology to match SWMM 4



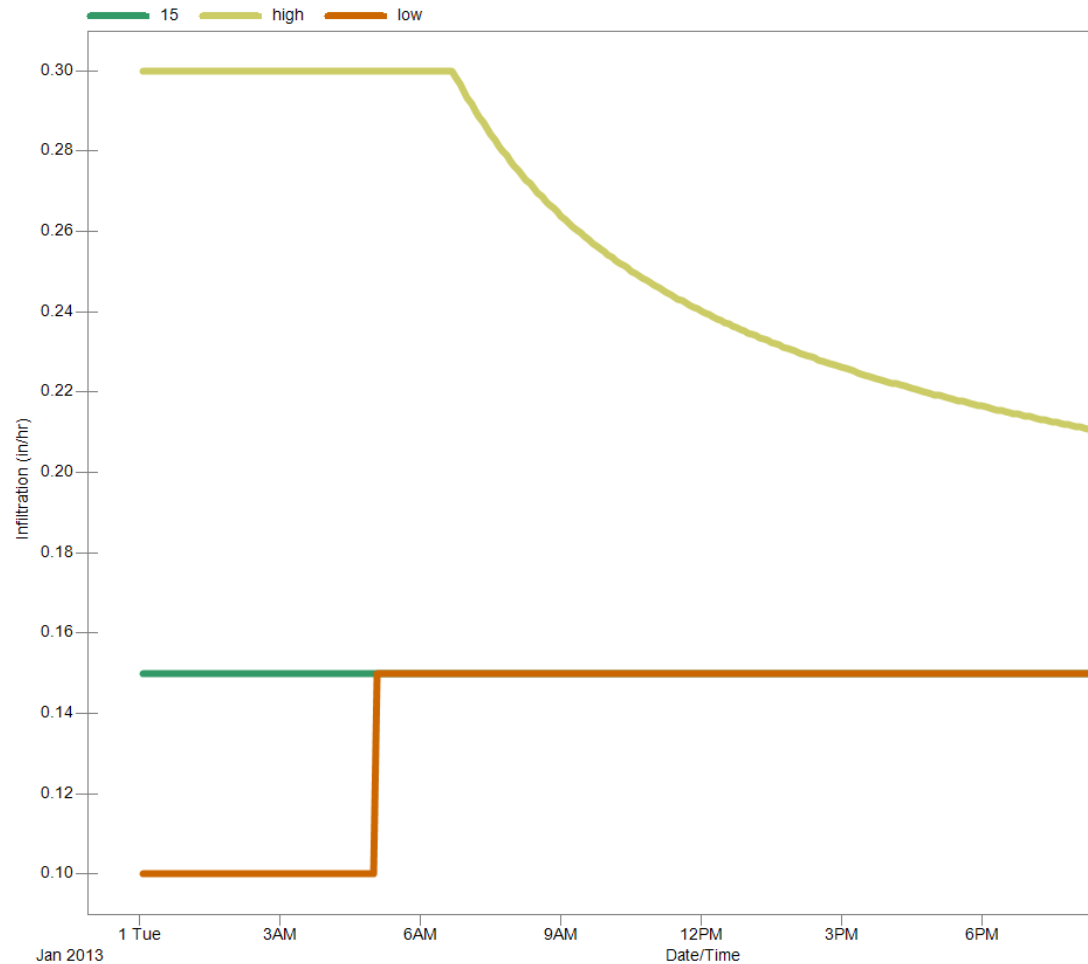
# Were there issues in SWMM 4? SWMM 3?

- At this point – Lew and others considered the problem solved. But...
- Our concerns were with the higher  $K_s$  values producing too little infiltration
- Now all  $K_s$  values in this range match the infiltration rate



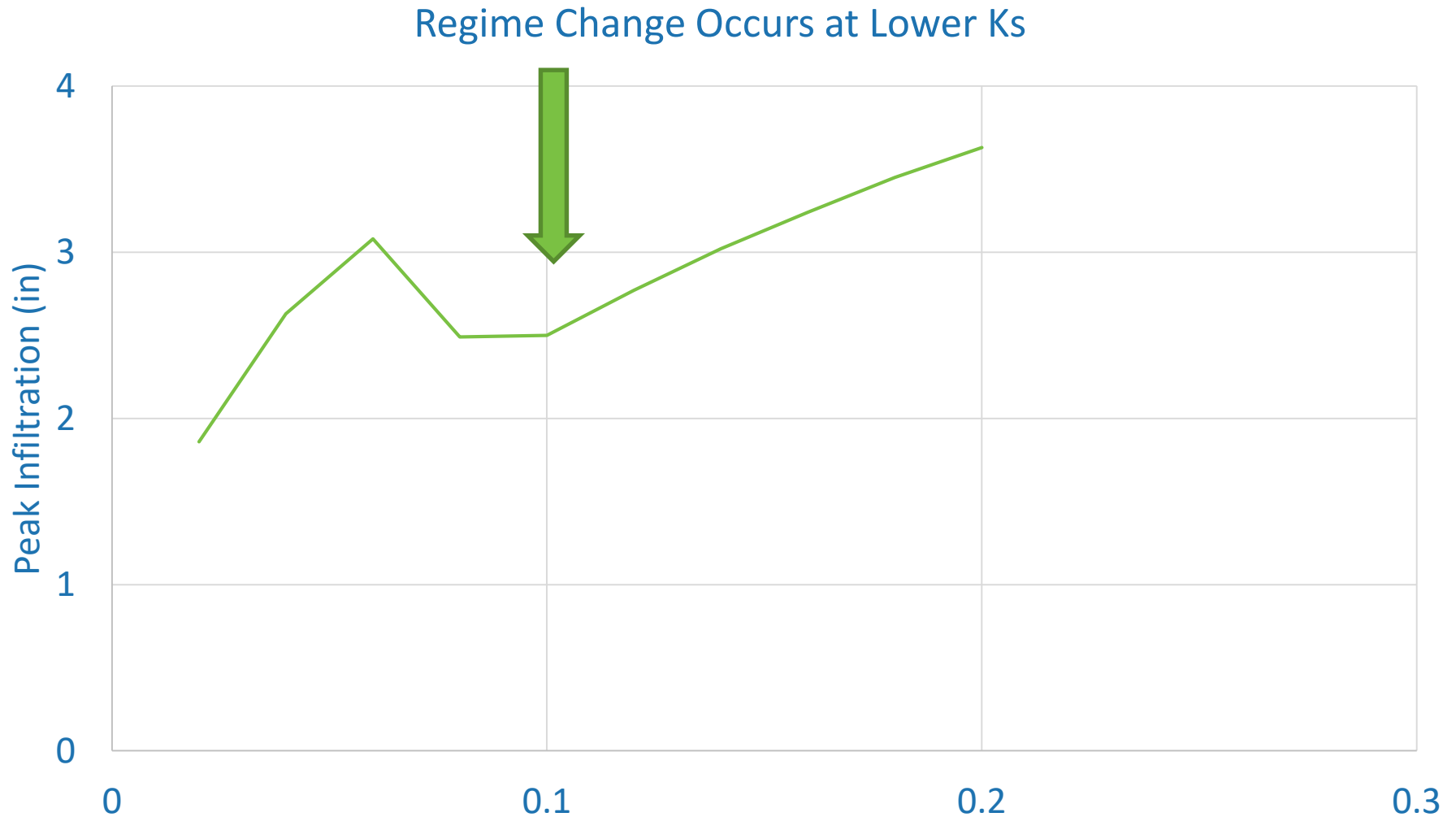
# Were there issues in SWMM 4? SWMM 3?

- Sensitivity test with three simple catchments, but varying rainfall
  - $K_s = 0.15$  in/hr, IMD = 0.25,  $S_u = 8$  in
  - “low” rainfall: 0.1 in/hr for 5 hours, then 0.3 in/hr
  - “15 ”  $i = K_s = 0.15$  in/hr for 5 hours, then 0.3 in/hr
  - “high” rainfall: 0.3 in/hr for the entire run





# Were there issues in SWMM 4? SWMM 3?



# The Issue

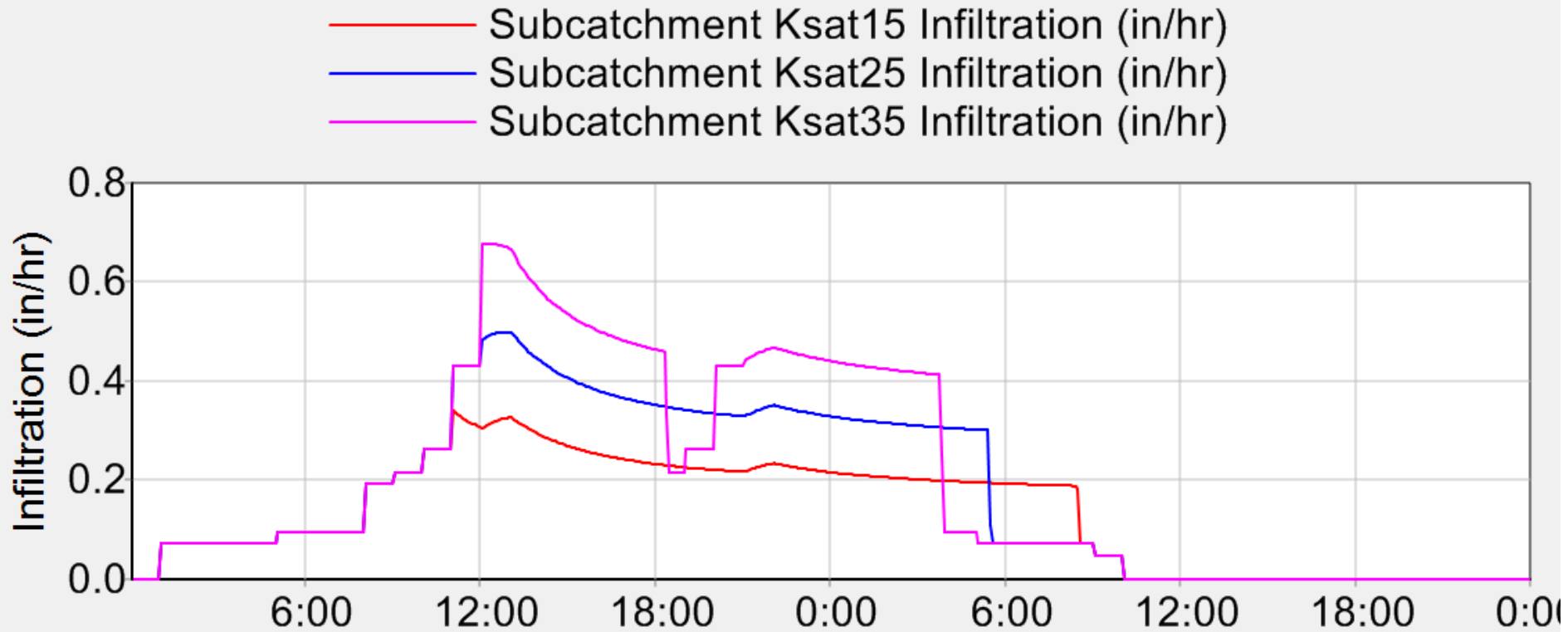
- The algorithm has two parts:
  - Mein-Larson estimate of infiltration
  - Soil moisture accounting
- In continuous simulation, soil moisture accounting drives estimate moisture deficit
- In NRCS design storm, moisture deficit driven to zero by low intensity rainfall well before peak

# The Solution

- Code revised so initial time remaining until next wet period set to large value
- At first time period where  $i > K_s$ , TR set as usual
- Since original method had been used for 30 years, we needed to research it more:
  - Followed up with Wayne Huber
  - Wayne Huber contacted Russell Mein

```
// --- rainfall does not exceed Ksat
if ( ia <= ks )                                     //(5.1.008)
{
    dF = ia * tstep;
    infil->F += dF;
    infil->Fu += dF;
    infil->Fu = MIN(infil->Fu, Fumax);
    if ( modelType == GREEN_AMPT && infil->T <= 0.0 ) // (5.1.010)
    {
        infil->IMD = (Fumax - infil->Fu) / infil->Lu;
        infil->F = 0.0;
    }
    return ia;
}
```

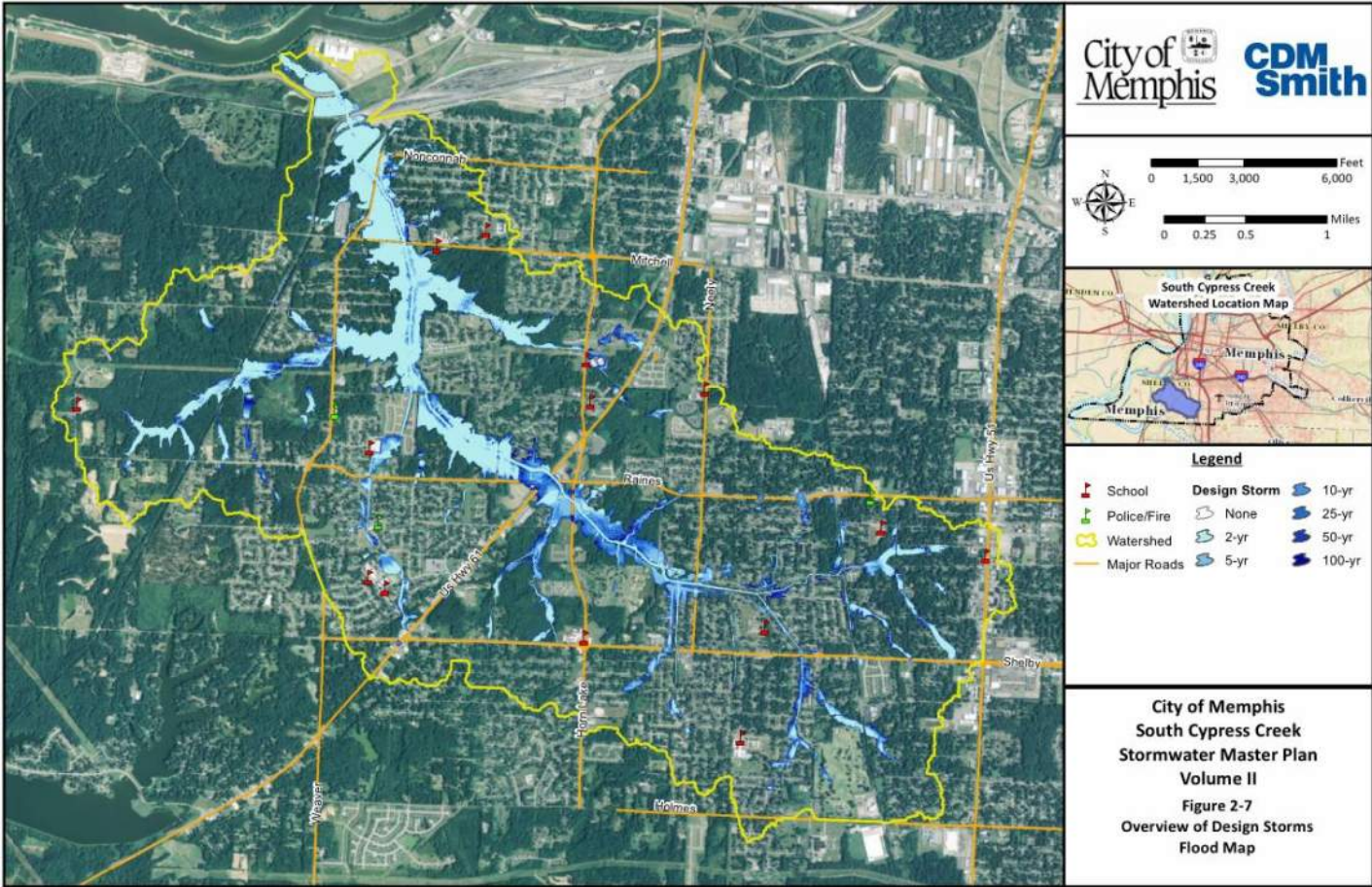
## Same test case – Modified GAML



# Test Case: Memphis South Cypress Creek

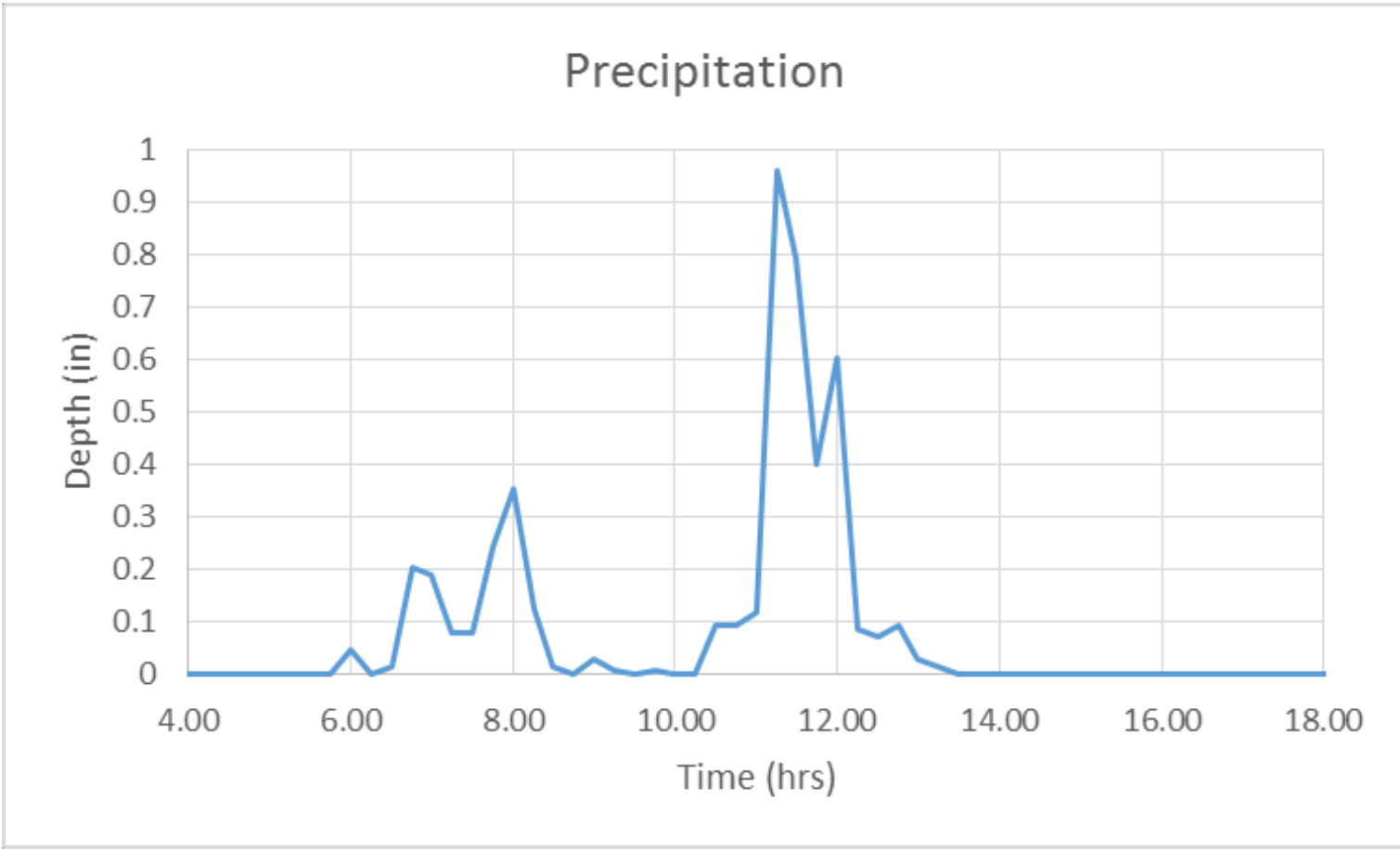
- 13 mi<sup>2</sup> with 179 subcatchments from 6.5 to 187.7 acres, averaging 46 acres

- 24% impervious
- Elev: 190 ft to 380 ft
- Soils from sandy loams to clay; 88% classified as B (Memphis Silt Loam)



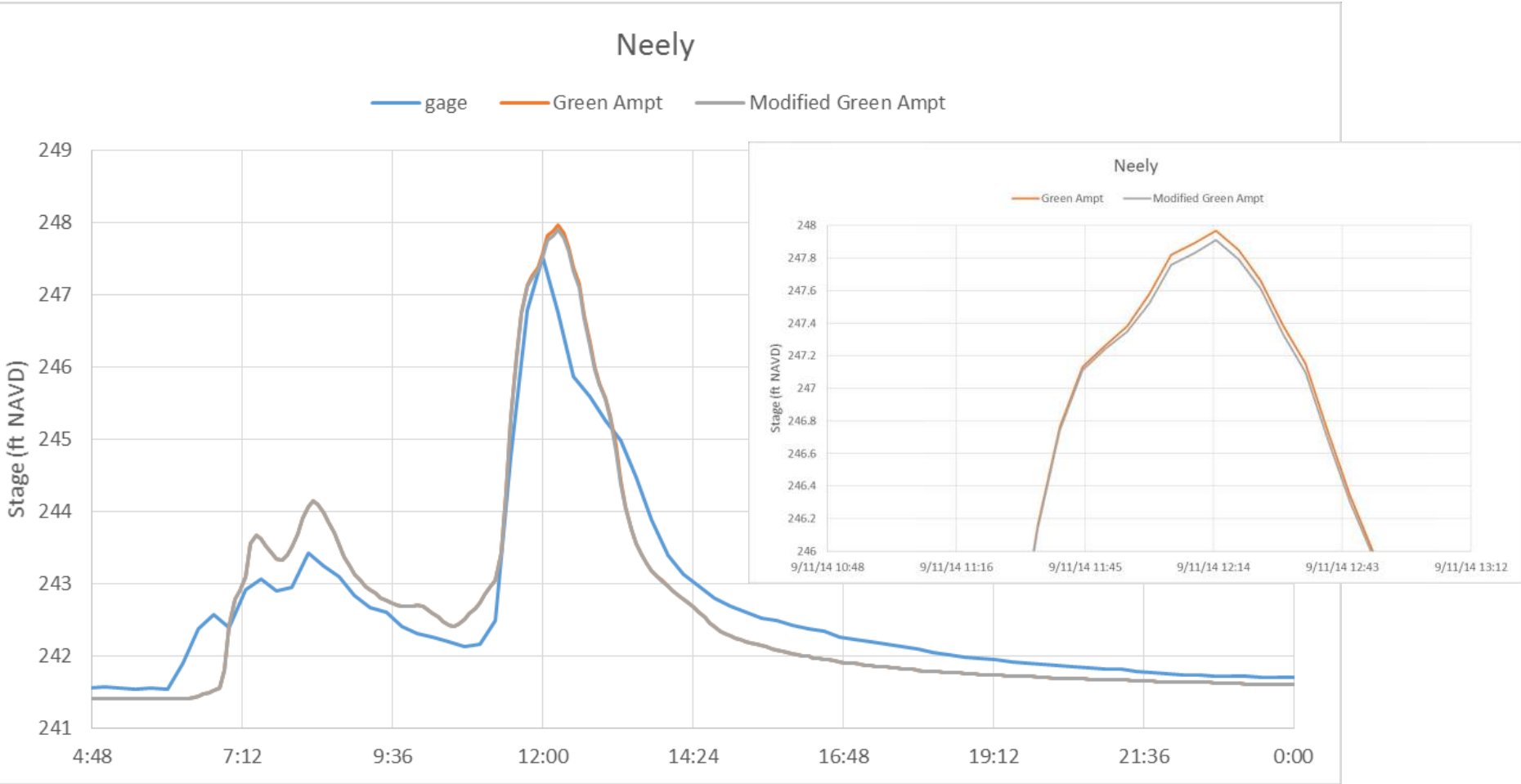
# September 2014 Storm

- 4.8-inch storm
- Peak Intensity ~ 1 inch in 15-minutes
- Dry antecedent condition



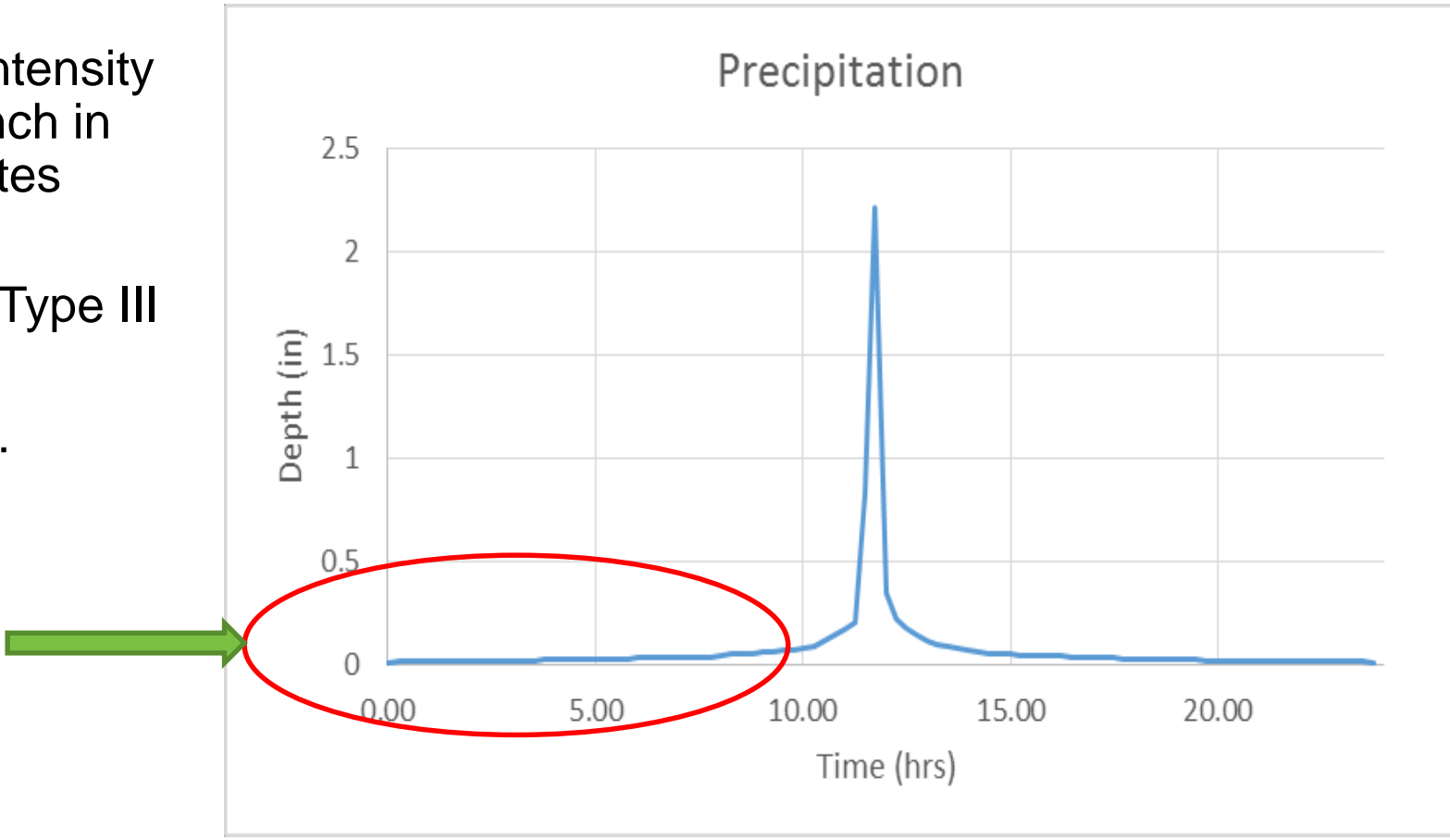
# September 2014 Storm

## — Stream Gage at Neely Road



# 100-Year Storm

- 8-inch storm
- Peak Intensity ~ 2.2 inch in 15-minutes
- NRCS Type III
- Issue...





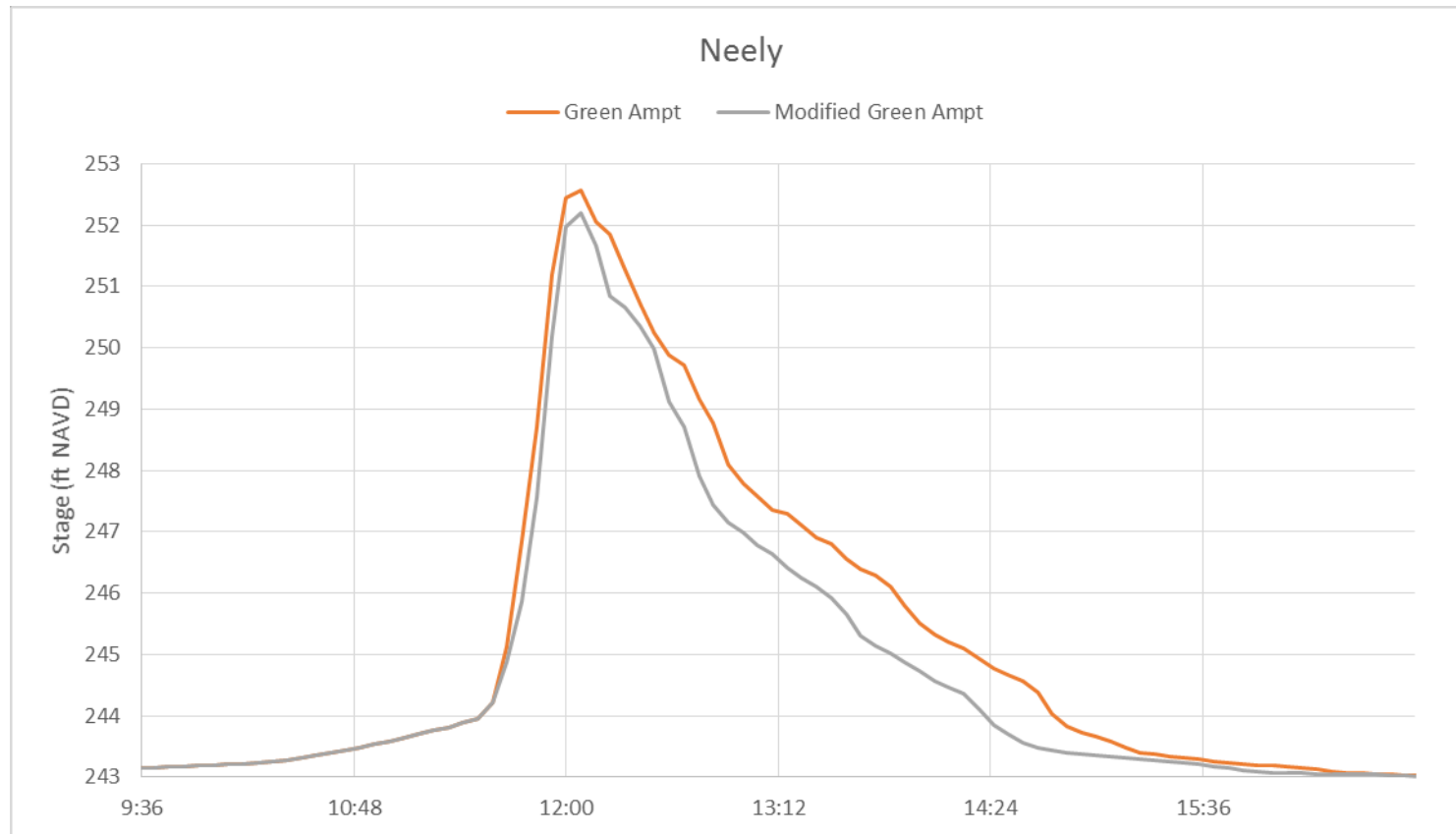
# 100-Year Storm

- Without infiltration cutoff at Ksat, infiltration increases 15% to 20% within the subbasins

- GA Peak  
Outfall Flow =  
9830 cfs

- Mod GA Peak  
Outfall Flow =  
8140 cfs

- 17% less



# Code revisions

-----  
Build 5.1.007 (9/15/2014)  
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## Engine Updates:

7. The initial cumulative infiltration into the upper soil zone for Green-Ampt infiltration had been incorrectly set to the maximum value instead of zero.
8. All of the Green-Ampt infiltration functions were re-factored to make the code easier to follow.

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Build 5.1.010 (08/05/15)  
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## Engine Updates:

1. A modified version of Green-Ampt infiltration (MODIFIED GREEN AMPT) was added that no longer redistributes upper zone moisture deficit during low rainfall events. The original authors of SWMM's Green-Ampt model have endorsed this modified version. It will produce more infiltration for storm events that begin with low rainfall intensities, such as the SCS design storm distributions.

# Conclusions

“I am impressed and pleased that there are people out there who keep checking model output. Unfortunately most model results are accepted by users without question” - Russel Mein